

# CHAPTER 3

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## Hand Gesture Recognition Based on Signals Cross-Correlation

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*“Any sufficiently advanced technology is indistinguishable from magic”  
Arthur C. Clarke*

Interactive gestures and body movements let us control and interact with mobile devices, screens and robots. Vision-based gesture recognition systems analyze the detected infrared and visible light after converting them into some measurable signal, e.g. voltage or current. Since, infrared and visible light are electromagnetic waves (EMW) with particular wavelength between 0.4 and  $1.6\mu m$ , we introduce a concept

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of a new kind of sensor for direct perception of EMW to see objects. We propose a novel framework for hand gesture featuring, profiling and recognizing based on signal processing and cross correlation of detected signals instead of Euclidean space analysis of image pixels by visual-based algorithms. Hand segmentation is accomplished on infrared radiation, while hand joints are categorized according to the intensity of visible light on hand edges. The meaning of a gesture is described by wave-based profiles representing the informative features of hand joints and their spatial relations over some period of time. A hand joint profile is a waveform of known shape obtained by superposition of feature waves. During the hand segmentation, we use online fuzzy clustering to categorize the infrared radiation. During the feature extraction, the clustering algorithm categorizes the grayscale light intensity on hand edges. During the training, the hand joint profiles are stored in the database as sampled sequences corresponding to the superposition of sine waves with amplitudes and frequencies derived from the obtained clusters. During the recognition phase, the current hand gesture is matched to the hand joint profiles in the database by fast signals cross-correlation. Our first implementation of the proposed framework inputs the raw data of Microsoft Kinect infrared and RGB image sensors that are wavelength dependent and produce a signal for electric current that is directly proportional to the changes in the focused flow of reflected light during hand gesturing.

### 3.1 Introduction

Interactive gestures are quite magical nowadays. They let us control and interact with mobile devices, screens and robots by air gestures, hands and body movements. The basic components of any gestural system [31] are presented in Fig.(3.1). A sensor is usually an electrical or electronic component, which detects changes in the environment. On detection it passes the information on to a comparator. It compares the current state to the previous state or the goal of the system and then makes simple or sophisticated decisions. A comparator is usually a micro-controller or mechanical systems that control gestures by transferring commands to an actuator. Actuators can be analog, like a small electric motor or digital, such as mobile software that changes the screen orientation from portrait to landscape.

Human-robot interaction (HRI) by gestures helps to personalize the communication with humans in various contexts and demands for a hand gesture recognition (HGR) system in real time. HGR systems can be classified into vision-based, infrared-based, electro-based, ultrasonic-based, accelerometer-based or wireless glove-based. The most popular sensors for robot vision are kind of cameras, like RGB, infrared depth (D), thermal or a combination of them. In recent years Microsoft Kinect sensor [7] for gesture recognition has been deployed widely for robots' vision. Although, Kinect is an RGB-D sensor providing synchronized RGB and depth images that overcomes the classical problems in computer vision concerning limitations of optical sensors sensitive to light illumination and cluttered background, it is questionable though, whether vision-based sensors and software is the most effective way for robots' vision and gesture recognition in terms of lightweight and fast processing of algorithms.

Real-world signals are analog. Not only the well-known electricity and magnetism

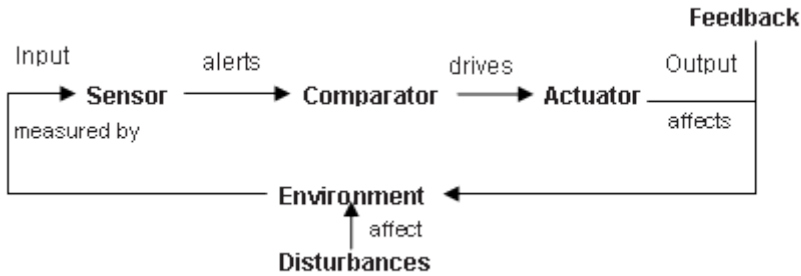


Figure 3.1: The basic components of any gestural system. (Image taken from [31]).

but light and heat are a measured response to continuously changes in energy levels of physical processes. Visible light (VL) and infrared (IR) are composed of electromagnetic waves (EMW) with wavelength ranging from  $0.4$  to  $1.6\mu m$  and the different colors of the VL are variations in the wavelengths. Do we need another kind of sensors for direct perception of electromagnetic radiation (EMR) to see objects? An interesting fact is that visual perception is mostly based on experience of the brain. For instance, the first days after birth babies see everything upside down. So, can robots learn how to reconstruct visual perception only by harvesting IR or VL analog signals? The concept we follow in this work is influenced by achievements in nano-technologies [8], nano-antennas [32] and interesting facts related to visions in some animals. Some animals use different eyes, organs like “Ampullae of Lorenzini” [1] in sharks, electroreceptive in fishes, pit organs and IR heat-sensitive membrane in some snakes [5] and organs in the mouth of platypus [26] to sense electro fields. Traditionally, waves are captured by antennas that convert EMR into some measurable signal, e.g. electric current. This naturally leads us to signal harvesting, processing and featuring by a grid of nano-antennas (nantennas) instead of Euclidean space analysis of image pixels.

The devices to detect VL and IR can be divided into three main categories: thermal detectors, quantum (photon) light detectors (QLD) such as a charge-coupled device (CCD) or a Bayer patterned sensor in digital cameras and radiation-field light detectors (RFLD), such as a very small antenna made-up with nanotechnology proportional to the length of light wave. Each type of light detectors is capable of sensing incident IR or VL radiation and converting it into some measurable signals. The last two detectors are wavelength dependent and they produce a signal for a current that is directly proportional to the response of changes in the focused flow of reflected light. QLD technologies exploit semiconductor devices for sensing VL or IR radiation, i.e., when subjected to light radiation, photons interact with electrons within the semiconductor to create mobile electric charges, while RFLD directly detect a radiation field similar to radio receivers depending on the frequency of the detected wave converting then the light into electrical signals. This naturally leads us to process and feature directly EMW. We propose a novel framework for hand gesture profiling and recognition based on signal processing and cross correlation of EMW instead of visual-based algorithms for image pixels analysis in space and frequency domains. Hand tracking is done by shining infrared light into the space around objects and nano-antennas capture re-

flections from IR or VL wavelengths. Hand segmentation is accomplished on infrared radiation; and based on it a set of monochromatic sensor data is separated for processing to decompose the hand in hand joints. A hand joint (HJ) is defined by its informative features - grayscale patterns on edges of the segmented hand. During the hand segmentation, we use online fuzzy clustering to categorize the infrared radiation and find the corresponding depth map and depth threshold where the hands are located. During feature extraction, we use online fuzzy clustering to categorize the light intensity on hand edges together with its spatio-temporal information. The meaning of a gesture is described by wave-based profiles of hand joints and their spatio-temporal relations. A hand joint profile is a waveform of known shape obtained by superposition of feature waves shifted by phase. During the training phase, the hand joint profiles are stored in the database (DB) of the robot as sampled sequences corresponding to the sum of sine waves with amplitudes and frequencies derived from the obtained clusters. Signals cross-correlation is used for matching of the observed waveform to the profiles in the DB.

The progress made by current research [32] indicating that RF concepts can be transferred to optical and infrared frequencies and the state-of-the-art works [15, 18, 24, 27] confirm that signal-processing algorithms for time series analysis might be a better alternative for hand gesture recognition. Time series analysis and measures are for acceleration signals [24], Doppler shifts along with Wi-Fi [27] or TV transmissions [18], as well as electrical fields to sense hand movements [15] instead of spectral, spatial and temporal models of regions in visual image sequences. In addition, signal-processing algorithms run faster than the pattern recognition techniques used in vision-based systems, since they require less preprocessing of the raw data and limited training phase. Moreover, pattern recognition based on waveforms cross-correlation is a function of a time-lag that can identify a short signal (feature) occurring in a long signal stream.

Although real-world signals can be processed in their analog form, processing signals digitally provide the advantages of high speed and accuracy. Often analog signals need to be processed so that the information they contain can be analyzed. Analog VL and IR signals can be converted to another type of signals that may be of use for HGR or changed to digital format by Analog-to-Digital Convertors (ADC) for processing by Digital Signal Processors (DSPs). After digitizing, DSP manipulates the signals mathematically and perform functions like "add", "divide", etc. It then returns the digitized information back to analog form through the use of a Digital-to-Analog Convertor (DAC) to be used in real world. As shown in Fig.(3.2), DSP information is used to control the robot hand. During the input phase VL analog signal might be harvest through a vision-based sensor (Kinect) or other detectors. This continuous signal is then converted to a digital form by ADC and passed to DSP. It performs signals "adding" and saves the complex waves into the memory. The output could be converted back to analog signal in real world or continue in the digital format for more complex DSP functions. For instance, DSP may compress signals so that they can be transmitted quickly without noise and interference from one place to another or can perform an interface for hand robot control.

Since the raw data obtained from Microsoft Kinect IR CMOS and Bayer patterned RGB sensors is wavelength dependent and produce a current signal that is directly proportional to changes in the focused flow of reflected light during gesturing, we

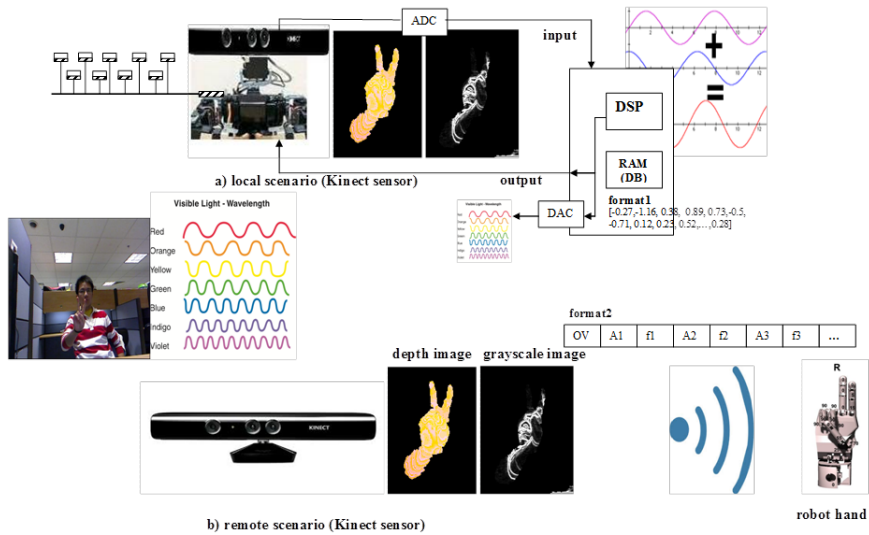


Figure 3.2: Signal processing in local and remote scenarios.

ask the following question: can we consider this spatial color detection in cameras organizing RGB colors on a square grid of photo sensors as a grid of wavelength dependent nano-antennas? The range around each photo detector keeps the electrical charge of which is initially fixed image and then sends it to ADC for analyzing analog pulses and converts them to digital format. The resulted intensity of current (IC) value corresponds to the intensity in light (IL) value in a specific position and each active element in the Bayer filter mosaic sensors is possible to be addressed individually.

The electric current charges of which is initially fixed image can be obtained from a new sensor for seeing gestures, presented in Fig.(3.3). It consists of a grid of nantennas (nodes) connected in a network in order to allow nodes communication in a local scope. Thus, distributed preprocessing of converted current signal from visible and infrared light will be performed. It is already known that RF concepts can be transferred to optical and infrared amplitudes and frequencies [32]. Figure 3.3a shows, for instance, 9 nantennas forming a  $3 \times 3$  grid, and an IR projector illuminating the object to detect depth and distinguish it from the background and interferences. The reflected VL and IR waves are converted to a current signal at each nantenna. Two major operations will take place: edge preprocessing and clustering.

For image recognition and pattern analysis, it is assumed that converting color image to grayscale has a little impact on recognition performance. A grayscale (monochromatic) image is a result of harvesting and measuring the intensity of light at each node in a single band of the electromagnetic spectrum, and the light intensity varies from black at the weakest to white at the strongest intensities. On the other hand, edge detection that operates on monochromatic light gives us the boundaries between related objects. Edges are informative enough for HGR and thus reduce the data to be processed. Edge detection algorithms accentuate regions that change greatly in

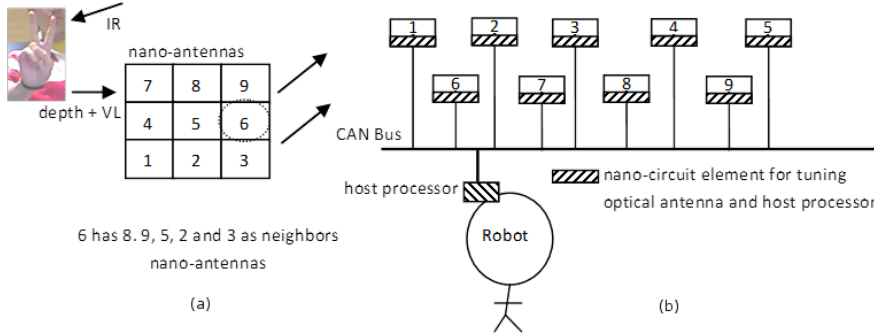


Figure 3.3: The architecture of a new sensor for seeing and recognizing hand gesture patterns: (a) the grid layout of nano-antennas and (b) the interconnection of grid to the CAN Bus.

intensity over short image distance and the most used algorithms are gradient-based, evaluating 2D gradient magnitude (GM) by  $3 \times 3$  square kernels. The purpose of the clustering is to categorize the input examples in fuzzy partitions resulting in overlapping clusters (features) for hand joints in terms of brighter and darker light intensity on edges in vicinity. We apply the online Low-complexity Constrained Fuzzy Clustering algorithm (LCFC) proposed in [21].

As shown in Fig.(3.3b), nantennas are connected through a communication hardware such as the CAN Bus [3], for instance. Nantenna nodes also communicate with each other by their IDs knowing their neighbors in  $x$  and  $y$  directions. Node ID is generated automatically as a function of the nantenna position in the grid. The preprocessing phase involves distributed edge detection with all one-hop neighbors. The clustering, on the other hand, consists in categorizing the IC on edges with more than one-hop neighbors and only if more clusters overlap, the IC of each cluster will be taken into consideration and sent for features, hand joints identification and profiling. Two approaches might be feasible to configure this new sensor - a distributed and a centralized.

In a distributed environment all the preprocessing and clustering are established at nantennas' level. The final results are sent via the CAN Bus to the robot for features post-processing. The algorithm for edge detection is distributed in all one-hop neighbors and can be described informally as: each node "telling the neighbors about its IC and GM". The algorithm is performed by each node in the grid, while clustering only by edge nodes. An edge node is a node, if its GM is non-zero (black color). The advantage here is that only a subset of nodes needs to know the IC or GM to detect edges or to perform clustering and clusters post-processing. Although the new promising paradigm for a nano-network [9] to organize the cooperation among nano-machines (tiny components consisting of an arranged set of molecules, which are able to perform very simple tasks), this phase is expensive, as it requires many nantennas to guarantee good quality, e.g.  $640 \times 480$  grid, additional hardware for each nantenna to perform communications and computations, plus the conversion of the

IC signal into digital form.

In a centralized environment, the nantennas have just nano circuit elements for tuning the optical nantenna and a host processor. The CAN controller connects them to the bus. The CAN (controller area network) bus is a vehicle bus standard designed to allow micro-controllers and devices to communicate with each other within a vehicle without a host computer but now it is widely used in other areas, as automation and medical equipment. Nantennas can send messages by the host processor to the robot that handles both pre-processing and clustering. Each node is able to send and receive messages, however not simultaneously. A message consists of node ID and payload up to several bytes. Distributed architecture implements threads. Every thread runs identical functions for cross-node communication, where nodes pass messages to advertise their IC and GM only to their neighbors. A node activates its own thread through a message. Thus robot will perform preprocessing and clustering in threads. For instance, 76800 threads will handle a  $320 \times 240$  grid of nantennas.

Identification and profiling of features and hand joints is performed on the robot side. During the training phase we perform reasoning process to decide whether the obtained clusters with close  $(x, y)$  coordinates are specific for a hand joint and how to label them together. First, we typify these features into sine waves with amplitudes and frequencies corresponding to the number of pixels and grayscale intensity of the cluster. We then superpose these waves shifted by phases (adjustment angles) to obtain the based waveforms for hand joints. The profiles can be described in two formats, either as sampled data sequences - the format1 in Fig.(3.8d) or a vector of ordered amplitudes and frequencies of participating features – the format2 in Fig.(3.8d). The DB consists of waveforms with known shape in format1. The format to be used depends on the environment of the HRI scenario as shown in Fig.(3.2). DSP hardware in a local scenario (Fig.(3.2a)) can be used by a robot to add and sample the features waves, as well as to perform cross correlation for measuring the HJ waveform for profiles in the DB. In a remote sensing scenario, see Fig.(3.2b), software sampler and adder are placed on a robot side and the features are transmitting wirelessly in format2.

In this chapter we propose a novel framework for hand gesture recognition extracted from different measurable signals that are proportional to infrared or visible light radiation combining: (1) distributed or centralized hand segmentation by categorizing IR light; (2) distributed or centralized edge detection; (3) distributed or centralized features extraction by online low-complexity constrained fuzzy clustering method to partition the intensity of light on edges in the segmented hand; (4) identification of typical hand joints clusters (features) in vicinity; (5) profiling of the hand joints as superposition of sine waves corresponding to parameters of overlapping clusters; (6) cross correlation function to match the observed complex wave to profiles for hand joints in the database; (7) formalism of Symbol Relation Grammar for a hand gesture description through the participating hand joints at the beginning and the end over a period of time, as well as (8) simple and fast bit-wise operations for matching the positioning relations of hand joints.

The remainder of the chapter is organized as follows: In Section 3.2 we review the related state-of-the-art systems. In Section 3.3 and Section 3.4 we present the basic concepts and models in the proposed HGR framework. In Section 3.3, we introduce the Kinect sensors specifications, how IR and RGB raw data are preprocessed, as well

as an overview of the used clustering algorithm. The innovation how hand joints profiles are represented by waves and signals cross-correlation for their classification are described in Section 3.4. Section 3.5 illustrates how to interface Kinect sensor with Action Script3 (as3). Software solutions for preprocessing of Kinect data and clustering of depth data are presented in Section 3.5.1, whereas experiments and results are described in Sections 3.5.2 and 3.5.3. Finally, the conclusion follows.

## 3.2 Related Works

In this Section we present the state-of-the-art work related both to Kinect based hand gesture analysis and signal-processing algorithms for time series analysis for hand gesture recognition.

First, we review some of the problems that researchers meet in using the Kinect sensor for HGR. The proposed online clustering algorithm, features identification and visual grammar formalism may resolve some of them. A comprehensive review of recent Kinect-based computer vision algorithms and applications can be found in [17]. Authors classify the state-of-the-art systems and approaches according to the type of vision problems that can be addressed or enhanced by means of the Kinect sensor. One of the covered topics includes hand detection, pose estimation and gesture classification. Hand detection and pose estimation can be accomplished either on depth images [10, 19, 20, 22, 28, 30, 34] or by combination of color and depth information [13, 25, 33]. The compromise is fast against precise algorithms. The most used depth similarity measure between observed and trained images is the inverse of their pixel-wise Euclidean distance. The used techniques for hand detection from depth images are simple heuristics [30, 34], distance invariant hand segmentation [10, 28] or clustering of the depth pixels [10, 20] followed by convex hull analysis [20], morphological constraints [10] or a Finger-Earth Mover's distance [30] to measure the dissimilarities between different hand contour/shapes. The critical part here is that depth threshold needs to be determined [34] to indicate the depth level where the hand is located or a variety of authors' assumptions need to be fulfilled, such as the hand to be the front most object or black belt equipped as in [30]. The often used models for 3-D pose estimation are: Particle Swarm Optimization [25], Support Vector Machine (SVM) to train and test from the obtained images features together with Hidden Markov Model (HMM) for relation between poses [33], and Random Decision Forest [19] to configure a skeleton-base pose. Hand detection based on depth data needs to be enhanced, since the resolution of the Kinect depth sensor is still limited and fingers tend to drop of the depth image because few light dots illuminate a finger far from the sensor. The hand detection can be enhanced by integrating color information [13] and motion detection based on frame differencing. Authors in [13] recognize gestures by Dynamic Time Warping (DTW) - a method that calculates an optimal match between two given sequences (e.g. time series) which vary in time or speed. DTW measure is used to match the similarity between two temporal time series of skeleton data in [29]. Hand gesture classification for pattern recognition targeting user-dependent gestures requires a training phase before use. The most popular approaches in literature for pattern recognition are HMM, DTW, Neural Networks (NN), Gaussian models, support



vector machines (SVM) and Bayesian networks. DTW is very efficient in operating with limited training data in contrast to HMM based methods which require extensive training in order to be effective.

Some interesting research for bringing gesture recognition on all devices use different sensors than vision-based and process analog signals. In [24] acceleration data is received in handheld devices for processing; Doppler shifts from the conventional wireless signals during gesturing is evaluated by Fourier analysis [27]; changes between signals in gesturing during TV transmissions (or Wi-Fi) is distinguished in AllSee [18]; electrical fields are sensed during hand movements by electrical-field-based 3-D gesture-controller integrated circuit [15]. The main advantage of signal-processing algorithms for hand gesture recognition like DTW and cross-correlation is that they run faster than the above mentioned pattern recognition techniques, since they require less preprocessing of the raw data and limited training, which is necessary and extensive for HMM, for instance. However, the amount of storage space used by the signal-processing algorithm grows as the number of features to be recognized increases, while it remains constant for HMM. The consumption of significant power and computational resources limit handheld devices applicability for gesture recognition. Always-on cameras and wireless receivers that require rich signal processing capabilities drain the battery, as well as computing FFTs and frequency-time Doppler profiles do. For that reason, AllSee extracts gesture information using simple rules that have minimal complexity to distinguish between signals in order to reduce the required signal processing capabilities. For example, to classify between the push and pull gestures, the rule is: if the maximum changes in the signal occurs closer to the start of a gesture segment, it is a pull action; otherwise, it is a push action.

The promising research in nanotechnology with optical and infrared nantennas based on metal nanostructures allow for efficient conversion of propagating light into nano-scale [32] will strongly enhance the radiation-field light detectors. As proposed in [32], nano-circuit elements and optical nantennas could be tuned to color variations in the wavelengths. With the first nano-networks test beds for molecular communication solutions [9], we can put the signal-preprocessing at nano-scale level and thus improve significantly the HGR time response, as well as save device resources.

Our approach outperforms the state-of-the-art systems in terms of accuracy, fast algorithm, simple hand joints profiling and classification based on signals cross-correlation. The used depth threshold for hand(s) location, which is calculated based on depth stream online and evolve, resolves some of the problems that researchers face when using Kinect sensor for hand gesture recognition. To the best of our knowledge, this is the first work involving hand gesture recognition based on a signal cross-correlation as a similarity measure between the observed and trained waves that profile the hand joints and their features in a novel way. We found two works where a cross-correlation coefficient is used as a similarity measure however, not as signals processing. In [11] for instance, it is used at feature extraction phase after image segmentation and morphological operation for hand gesture extraction. Authors in [29] denote a set of feature time-series obtained from skeletal motion and use a distance metric based on DTW. We first introduce a concept for a new sensor for seeing hand gestures by a grid of IR and VL wavelength dependent nantennas and preprocessing the converted waves to current signal light in a distributed way at the nantennas level.

### 3.3 Hand Gesture Recognition Framework: Preprocessing and Categorizing of Raw Data

In this section we present the Kinect sensors, IR and RGB data preprocessing, an overview of the online low-complexity constrained fuzzy clustering algorithm and post-processing of clusters in vicinity.

Our first implementation of the proposed HGR framework exploits as inputs the raw data from Microsoft Kinect infrared depth and Bayer patterned RGB image sensors, see Fig.(3.2). We assume that with a small amount of quantization error, we can extract the amplitude and frequency for VL and IR signals from these data since visual-based sensors are wavelength dependent and produce an electric current that is directly proportional to changes in intensity of light. Addressable photo sensors are grouped in a square grid and electric current charges are converted into digital image format by ADC. The resulted RGB value corresponds to the light intensity in a specific position. We apply the centralized approach for preprocessing and clustering of light intensity. Grayscale model is synthesized from the RGB and passed as an input to edge detection algorithm. Then edges are converted to monochromatic HSV (hue, saturation and value) model and passed as an input to clustering algorithm. The overall process flow in hand gesture recognition framework using Microsoft Kinect sensor as shown in Fig.(3.4).

#### 3.3.1 IR and RGB Raw Data and Video Streams From Kinect Sensor

Real-time hands gestures' recognition is a challenging task because there are thousands of different hand directions, sizes and shapes. The advent of quite cheap color image and depth sensors have aided research in this field. One of the most popular devices is Microsoft Kinect sensor [7]. Details about its hardware specifications can be found in [17, 6]. The depth sensor captures video data in 3D under any ambient light conditions and provides raw depth data, from which we identify the pixels of segment hands. It consists of an infrared laser projector combined with a monochrome CMOS sensor. The monochrome depth sensing video stream has a VGA resolution of  $640 \times 480$  pixels with 11-bit depth, which provides 2,048 levels of sensitivity. The Kinect can stream the view from its IR camera directly, see Fig.(3.5a) before it has been converted into a depth bitmap as shown in Fig.(3.5b). The default RGB video stream uses 8-bit VGA resolution of  $640 \times 480$  pixels with a Bayer color filter. The hardware is capable of resolutions of up to  $1280 \times 1024$  (at a lower frame rate) with other color formats such as UYVY. The Kinect sensor has a practical ranging limit of 1.2–3.5m distance. Kinect's various sensors output video at a frame rate of  $\sim 9Hz$  to  $30Hz$  depending on the set up resolution [6].

Hands can be detected on depth or RGB data. Sometimes, the accuracy of hand detection needs to be enhanced by integrating the synchronized to depth map color information. We use the skin color regions and center of gravity statistic to refine where the hands are located. Using the Microsoft Kinect skeleton joints model for detecting where the hands are located is a particular case and not applicable for general use of the proposed HGR framework.

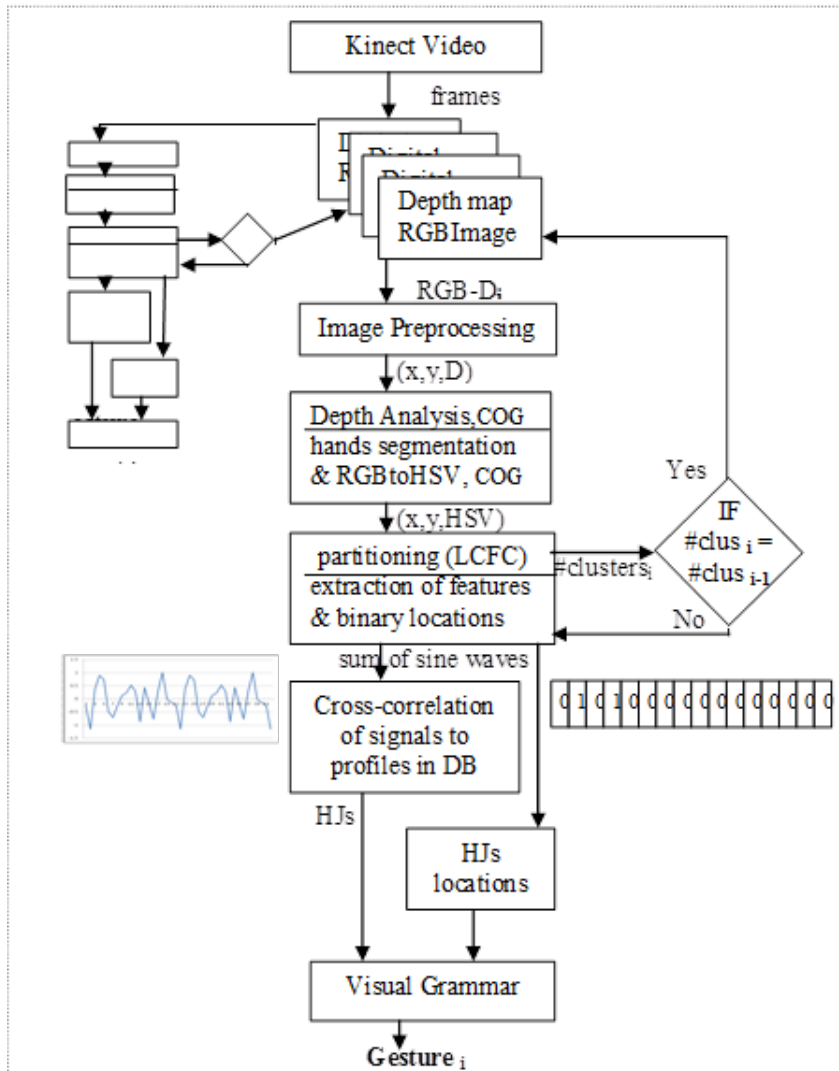


Figure 3.4: Overall process flow in hand gesture recognition framework.

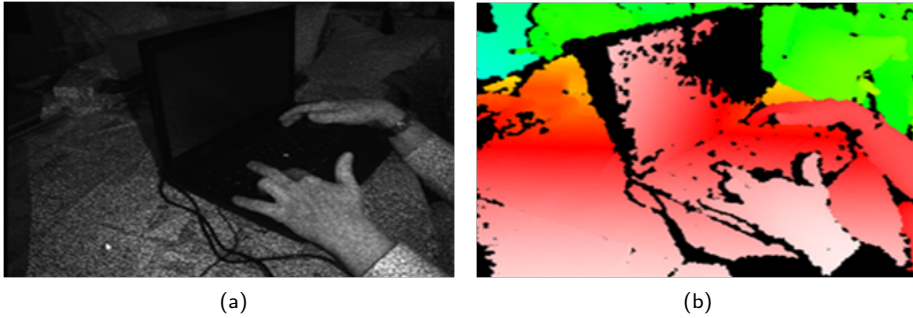


Figure 3.5: Kinect stream from IR camera and converted into a depth map (Images taken from [6]): (a) IR image shows the laser grid Kinect uses to calculate depth and (b) a depth map is visualized using color gradients from white (near) to black (far).

By analogy to Kinect skeleton joints we define 16 hand joints: 10 for fingertips for both hands, and correspondingly 2 for left and right wrists, fists and palms. The HGR framework allows a new joint type to be easily inserted. Examples for hand joints variables are presented below:

```
Joint palm_l=hand.Joints[JointType.PalmLeft];
Joint fist_l=hand.Joints[JointType.FistLeft];
Joint fngtip_t_r=hand.Joints[JointType.FingerTipThumbRight];
Joint fngtip_1_r=hand.Joints[JointType.FingerTipPointingRight];
```

The hand joints' identification is built on the depth data processing, color vision algorithms, machine learning by fuzzy clustering and reasoning process on overlapping clusters.

## 3.3.2 Preprocessing of Depth and RGB Raw Data

### 3.3.2.1 Preprocessing of a depth stream

Hand segmentation is accomplished on infrared radiation converted to depth map. The used technique here for hand detection from depth map is a simple heuristic over depth stream or clustering. In a scenario where the hands are the most front objects, we can find the minimum depth ( $D_{min}$ ) and process only the depth values up to the  $D_{min}$  plus  $90 - 100mm$  (established during our experiments in "Kinect near mode") to define a depth threshold ( $D_{thr}$ ) for the pixels to be processed. Let  $BMD\_D(x, y)$  be the output depth binary bitmap image data and the  $D(x, y)$  is the depth value of the pixel at  $(x, y)$  position. When  $D_{min} > D(x, y) < D_{min} + D_{thr}$  we consider the pixel as hand-like, otherwise we set  $BMD\_D(x, y)$  to 0 (black color) to isolate this pixel. For more precise classification of the hand-like pixels we use LCFC algorithm. After clustering the pixels in the depth map, we distinguish between fingertips and palm or fist by simple rules considering COG and radius of the clusters. More details

$$\begin{aligned}
 R' &= R/255 \\
 G' &= G/255 \\
 B' &= B/255 \\
 C_{max} &= \max(R', G', B') \\
 H=0^\circ; S=0\%; V &= C_{max}\%
 \end{aligned}$$

Figure 3.6: RGB to HSV color conversion for gray colors.

about the clustering algorithm and its parameters are presented in Section 3.3.4, while AIR Kinect software solution for clustering of depth data is discussed in Section 3.5.1.2.

In a scenario where a hand is not the front most object, the segmentation is aided by RGB skin detected regions. We calculate COG (see next subsection) of the segmented skin-like regions and use it in the reasoning process to ignore other body parts or noise, e.g. an object with the same depth values.

### 3.3.2.2 Preprocessing of RGB to monochromatic intensity of light

Each RGB pixel is transformed to HSV model before converting it to grayscale. Hue and Saturation channels are used for detecting the skin-like regions using predefined thresholds. We apply the commonly used HSV threshold values that are good for most images (H has to be normalized by 360):  $H_{min} = 0$ ,  $H_{max} = 0.14$ ,  $S_{min} = 0.2$  and  $S_{max} = 0.68$ ;  $V_{min} = 0.36$  and  $V_{max} = 1$ . For dealing with different skin color of people these thresholds vary. Let  $BMD\_HSV(x, y)$  be the output binary bitmap image data and the  $H(x, y)$ ,  $S(x, y)$  and  $V(x, y)$  are the hue, saturation and value of the pixel at  $(x, y)$  position. When  $H_{min} > H(x, y) < H_{max}$  &  $S_{min} > S(x, y) < S_{max}$  &  $V_{min} > V(x, y) < V_{max}$  we consider the pixel as skin-like, otherwise we set  $BMD\_HSV(x, y)$  to 0 (black color) to isolate this pixel.

We convert then the hand-like regions into a grayscale model. Monochromatic (grayscale) images are a result of measuring the intensity of light in a single band of the electromagnetic spectrum, i.e., monochromatic light is when only a given frequency is captured. The grayscale bitmap can be synthesized from a RGB image, as shown in Fig.(3.6). Gray colors have an equal amount of red, green and blue color levels in the range  $[0, 255]$ . Only V channel is important in HSV model for shades of gray.

We then apply a Sobel gradient based method [14] for edge detection. An edge is the boundary between overlapping objects and we exploit it for hand joints identification. The Sobel operator performs a 2-D gradient measurement on an input grayscale image to accentuate regions that change greatly in intensity over short image distances. These regions correspond to edges. To find the absolute gradient magnitude at each point, Sobel uses a pair of  $3 \times 3$  convolution masks (kernels). The first estimates the gradient in the  $x$ -direction, while the other finds the gradient in the  $y$ -direction. These kernels are designed to respond maximally to edges running vertically and horizontally relative to the pixel grid manipulating a square of pixels at a time and are combined together to find the absolute gradient magnitude at each point. The Sobel convolution kernels are shown in Fig.(3.16a) in Section 3.5. The as3 source code for implementation of Sobel algorithm is given too. Other  $3 \times 3$  and  $5 \times 5$  gradient operators for edge detection are also very popular, such as Prewitt and Scharr and could

```

For each pixel (x, y) calculate:
cogX=cogX+((r+g+b)/3)*x;
cogY=cogY+((r+g+b)/3)*y;
accumRGB += (r+g+b)/3;
cogX=cogX/accumRGB;
cogY=cogY/accumRGB;

```

Figure 3.7: Pseudo code for Center of Gravity (COG\_rgb) statistic calculation.

be exploited, as well. We tried simpler algorithms for edge detection with only one  $5 \times 5$  kernel, however it did not provide a good edge resolution resulting in clustering with less accuracy.

After the hand segmentation, we use a center of gravity (COG) statistic, i.e., where the COG of the segmented hand lies. Its purpose is to ignore the noise from background pixels with the same IR (depth) values or to find the coarse orientation of the hand. We propose two approaches for calculating COG: (1) from depth bitmap - COG\_D or (2) from RGB skin-based bitmap - COG\_rgb like in [23]. Instead of performing burden bitmap analysis to get the COG\_rgb, a quick row data in depth map is spatially analyzed by LCFC. For more details see Section 5.1.2. We find COG\_D by coarse clustering with big DM threshold as 0.3, which results in one cluster with centroids defining the COG\_D. For more precise estimation of  $Dthr$  we can vary the millimeters that we add to  $Dmin$  until COG\_D gets equal to COG\_rgb. In a scenario where the hands are not the most front objects, we use the second approach and formulae given in Fig.(3.7). It tolerates brighter pixels and they have more impact on the final COG\_rgb location than darker pixels. Thus  $Dthr$  evolves with each frame.

### 3.3.3 Feature Extraction

#### 3.3.3.1 Overview of low-complexity constrained fuzzy clustering algorithm

Our feature extraction is based on distance-based fuzzy clustering. The most often used distance-based clustering like CMeans and k-Mean are offline. A priori threshold value defines when a cluster is to be updated or new cluster is to be created. Human-robot interaction by a vision-based gesture interface needs online clustering process. Estimating the number of clusters online will help in online optimization of the threshold value and the radii of the clusters. We apply online low-complexity constrained fuzzy clustering algorithm to partition the coordinates and the V value of edge pixels normalized in  $[0, 1]$  range. The main idea is to localize specific small grayscale regions by categorizing the values of edge pixels. The overview of LCFC algorithm is presented in details in [21]. For more details about implementation, see Section 3.5.1.2.

In the online clustering process, the given data set consists of input vectors  $X = \{x_1, \dots, x_p\}$ , which are  $p$  points in  $q$ -dimensional space. In the present application  $p$  is the number of pixels to be processed, while  $q$  is 3, referring to the three dimensions of each pixel that we take into consideration -  $(x, y)$  coordinates and the V channel. The algorithm starts with an empty set of clusters. When a new cluster  $C_k$  is created ( $k$  is an index related to the time instant), the current input vector is assigned to

be a cluster center ( $C_c$ ) and its cluster radius ( $Ru$ ) is initially set to zero. Then this cluster is updated or new cluster is created depending on online decision using equations Eq.(3.1) and Eq.(3.2). Euclidean distance to mean centers ( $Mc$ ) together with fuzzy membership degree ( $Md$ ) of the input vector to each cluster participate in the updating or creating of a new cluster. The two smallest distances from the input vector to reference centers  $Mc_j$  participate in the denominator of Eq.(3.2). The *reference center* is described by the arithmetic mean of coordinates for all classified inputs to the  $j^{th}$  cluster by Eq.(3.1).

$$Mc_j = \sum_{i=1}^{cp} s_i / cp \quad (3.1)$$

where  $s_i \in \mathbb{R}^q$  are the classified inputs to  $j^{th}$  cluster and  $cp$  is their number

$$Md_{ij} = \begin{cases} 1 - \min(\|x_i - Mc_j\|)^{\left(\frac{2}{m-1}\right)}, & n = 1 \\ \frac{1}{1 + \frac{\min_1(\|x_i - Mc_j\|)^{\left(\frac{2}{m-1}\right)}}{\min_2(\|x_i - Mc_j\|)^{\left(\frac{2}{m-1}\right)}}} & , n > 1 \end{cases} \quad (3.2)$$

where  $x \in \mathbb{R}^q$  and  $m \in [1, \infty)$  is the weighted exponent coefficient which determines how much clusters may overlap. We set  $m$  to be equal to 2.

The acceptable tolerances to  $Mc$  and  $Md$  are expressed by two thresholds:  $Md$  threshold ( $Mdthr$ ) and Mean Threshold ( $Mthr$ ). When  $Md$  is less than  $Mdthr$  or  $DMc_{ij}$  is bigger than  $Mthr$  we create a new cluster, otherwise we can increase the radius of this cluster. The idea is cluster radii not to be updated anymore when: (1) an example is close to more than one cluster; (2) the examples classified to cluster  $j$  are concentrated in the far half of this cluster with a big radius. The two thresholds are in the range of  $[0, 1]$  and are very intuitive for tuning. When  $Mdthr$  has values in the range of  $[0.4, 0.5]$  the clusters are well partitioned. By varying  $Mdthr$  we perform coarse or fine clustering. When  $Mthr$  has values in the range of  $[0.4, 0.6]$  the data are partitioned close to optimal and usually the same clustering centers are obtained for several close threshold values. Big values for  $Mdthr$  and small values for  $Mthr$  result in a big number of clusters.

### 3.3.3.2 Thresholds for clustering of depth and RGB raw data

During the clustering of depth data, the input data to LCFC is as  $x$ ,  $y$  and  $D$  values obtained from depth stream. As we noted in Section 3.3.2.1 we use coarse clustering with  $Mthr$  threshold 0.3 to find COG\_D and fine clustering with  $Mthr$  threshold in the range of  $[0.05, 0.07]$  to categorized fingertips and palm/fist.  $Mdthr$  threshold is 0.4. During the clustering of RGB data, the input data to LCFC is  $x$ ,  $y$  and  $V$  value obtained from HSV model.  $Mthr$  is in the range of  $[0.08, 0.12]$  resulting in about 30-40 clusters.  $Mdthr$  threshold is in the range of  $[0.4, 0.5]$ .

### 3.3.4 Post-processing of Clusters

We perform reasoning process after online fuzzy clustering in the regions with high change in light intensity that corresponds to edges of the segmented hand. We define a neighborhood mask by analogy to neighbors in a communication network in  $n$ -hops that will perform this operation in a distributed way. Network nodes communicate with each other by their IDs and know their neighbors in  $x$  and  $y$  directions. Node ID is generated automatically as a function of the node position in the grid. For instance, 124 antennas forming an  $18 \times 8$  grid and the node (cluster centroids) communicate more or less with the neighbors in 9 hops horizontally and 4 hops vertically. Thus we manipulate  $r \times c$  nodes ( $r$  neighbors horizontally and  $c$  neighbors vertically) relative to the adjacent segmented hand grid, referred to Fig.(3.9a). The neighborhood mask is usually much smaller than the segmented hand image, see Fig.(3.9c). We start from first cluster centroids and take over with the others to find all places where more than four clusters overlapped avoiding clusters with light intensity less than 0.1 as it is not really informative. As a result, we propose grayscale patterns with a potential to be typical for a hand joint features. Grayscale patterns consists of averaged V-values for the neighbor nodes (pixels) but are transmitted for processing during the training or testing phases together with the number of participating in the clusters nodes (pixels), as well as with the spatial information of the clusters centroids. The cell(s) in the adjacent grid where the neighborhood mask finds overlapping defines the HJ position.

## 3.4 Hand Gesture Recognition: Features and Hand Joints Identification, Profiling and Classifications

In this section, we show how monochromatic light intensity in vicinity (features) and profiles of hand joints are represented by waves and signals cross-correlation for their classification, how hand joints are positioned in the HGR framework and then how VG is applied for hand gesture description and recognition.

### 3.4.1 Features and Hand Joints identifications and profiling

We search for clusters that are typical for the hand joints containing brighter and darker pixel information. A human eye can't distinguish the gray shades, as the LCFC algorithm does, even though they exist. In Fig.(3.8), we hardly distinguish seven overlapping clusters in the right fingertip. With the help of LCFC algorithm results, we found out that the averaged V channel for the fingers show density of clusters for brighter and darker pixels in the neighborhood with radii about 16 pixels (in other words - many edges with different grayscale level are placed at the overlapping locations). Thus we defined the size of the neighborhood mask to be  $19 \times 9$ . We use these observations for features division and established several ranges for the averaged gray level of the edges for neighbor pixels, in which the probability to identify a specific feature is high. To avoid misclassification, we take into consideration all the clusters in the neighborhood mask. For instance, the averaged gray level of pixels around the pointing finger or thumb has V-values in the range of  $[0.07, 0.3]$  and  $[0.6, 0.8]$  at



almost the same coordinates.

The main idea in feature and HJ profiling is associated with identifying clusters with specific light intensity on edges of hand joints to represent each feature as a wave. Visible light is EMW with frequency range of the visible spectrum from 405 to 790 Terahertz (THz) and each signal can be represented as a Fourier series. Colors are variations in RGB frequencies. The red, green and blue frequencies correspond to 430, 560, 660 THz. The monochromatic intensity (gray shades) has its own frequency, as well, an equal amount of R, G and B. As shown in Fig.(3.6), only V channel is important in HSV model for shades of gray. For instance:

RGB hex code #989898	RGB(152,152,152)	HSV(0°,0%,59.6%)
RGB hex code #D0D0D0	RGB(208,208,208)	HSV(0°,0%,81.6%)

We typify the grayscale patterns (the features) as a sine wave since intensity of the electric current captured by the detector which represents the converted visible light, is a simple periodic signal. For the sake of simplicity, according to the cluster parameters and following the principle of superposition, we characterize clusters in the vicinity as a waveform obtained by a combination of sine waves shifted by phase. An illustration on how the edges of the segmented hand, overlapping clusters and gray patterns look like is presented in Fig.(3.8). Simple sine waves correspond to each cluster (feature) for the pointing finger, see Fig.(3.8a). The complex waveform shown in Fig.(3.8c) is one of the profiles in the database for pointing fingers.

Mathematically, the most basic wave is the one-dimensional sine wave (or sinusoid). It is a mathematical curve that describes a smooth repetition of oscillations. Its most basic form as a function of time ( $t$ ) is described by Eq.(3.3) :

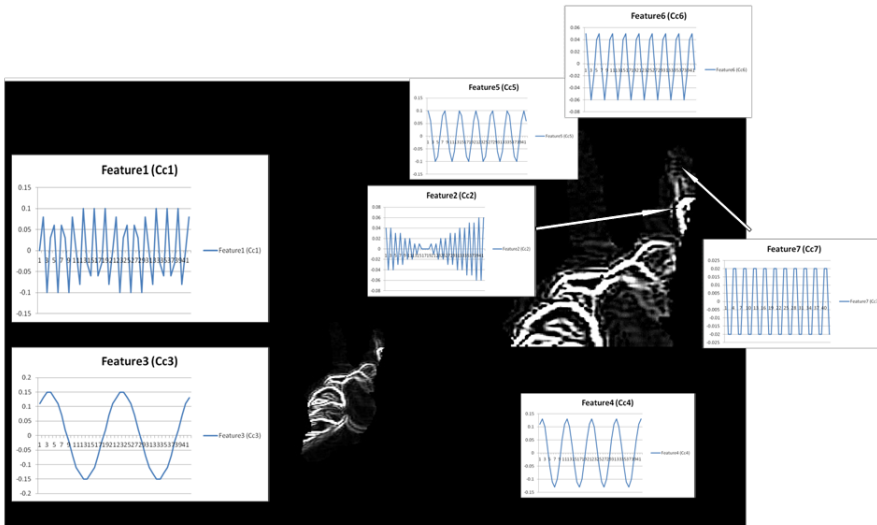
$$y(t) = A \sin(2\pi ft + \phi) \quad (3.3)$$

where

$A$  is the amplitude (the peak deviation of the function from zero),  
 $f$  is the frequency (the number of oscillations that occur per second),  
 $\phi$  is the phase, specifies in radians.

When  $\phi$  is non-zero, the entire waveform appears to be shifted in time. A negative value represents a delay, and a positive value represents an advance.

Equation 3.3 is enough to represent the intensity of the current captured by the sensor which represents a simple periodic signal. We epitomize the intensity of the gray color in each cluster as the frequency of the sine wave. We take into consideration the number of participating pixels in the cluster (correspondingly the number of antennas from which this gray intensity in the cluster is obtained), as well as a phase abstraction representing an advance in time that sinusoids for right handed positioning clusters (ordered by  $x$  coordinate) have. As an alternative, features might be ordered by their  $y$  coordinates. The number of examples in each cluster corresponds to wave amplitude, frequency associated with intensity of gray color, and phases distinguishing how the waves are to be superposed in time. We then compose a complex waveform by superposition of individual for features sine waves. Thus a hand joint profile is a



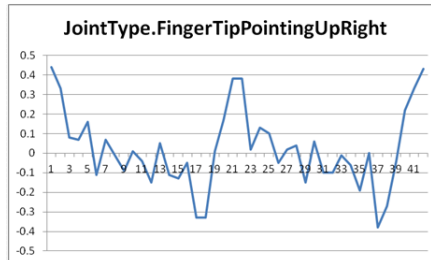
a) simple sine waves corresponding to each cluster (feature) of the pointing finger

```

LCFC output: 7 overlapping clusters
30 pixels X 0.474761 Y 0.6055661 color 0.666
28 pixels X 0.492406 Y 0.601399 color 0.96432
45 pixels X 0.497085 Y 0.5771614 color 0.0727
40 pixels X 0.49833 Y 0.5916701 color 0.1533
29 pixels X 0.50059 Y 0.5884475 color 0.22197
19 pixels X 0.503232 Y 0.5891273 color 0.3156
9 pixels X 0.505825 Y 0.5929165 color 0.46829

```

b) 7 clusters for the pointing finger

c) superposition of sine waves for the pointing finger shifted by phases  $0\pi$ ,  $\pi/6$ ,  $\pi/4$ ,  $\pi/3$ ,  $\pi/2$ ,  $2\pi/3$ ,  $3\pi/4$ .

```

format1[0.44,0.33,0.08,0.07,0.16,-0.11,0.07,-0.01,-0.09,0.01,-0.04,-0.15,0.05,-0.11,-0.13,-0.05,-
0.33,-0.33,0.01,0.17,0.38,0.38..]

```

```

format2
[A1=0.1, f1=0.7; A2=0.09, f2=0.96; A3=0.15, f3=0.1; A4=0.13, f4=0.2; A5=0.1, f5=0.3; A6=0.06, f6=0.4;
A7=0.03, f7=0.5]

```

d) Hand Joint formats

Figure 3.8: Edges of the segmented hand and features and HJ profiling and formats.

waveform of known shape  $S(t)$  obtained by summing of individual sine waves with amplitudes  $A_i$  and frequencies  $f_i$  corresponding to the amplitudes and frequencies derived from the obtained clusters and shifted by phase with increasing positive values for  $\pi$  correspondingly to their locations, e.g.  $0\pi, \pi/6, \pi/4, \pi/3, \pi/2, 2\pi/3, 3\pi/4, 5\pi/6, \dots$  as presented by Eq.(3.4). The number  $S$ , corresponding to the number of overlapping clusters, defines the number of sine waves to be summed, and  $n$  is the number of samples.

$$S_n(t) = \sum_{i=0}^S A_i \sin(2\pi f_i t_n + \phi_i) \quad (3.4)$$

where  $i = 1, 2, \dots, S$  and  $n = 1, 2, \dots, N$  and

$$\begin{aligned} t_n &= t_{n-1} + t_1 \\ t_1 &= \frac{1}{2f_{max}} / precision \end{aligned}$$

During the training phase, the database has to be fed with such hand joint profiles. However, since the  $S(t)$  is a continuous signal, we need to quantize it into digital numbers that represent the quantities. The conversion rate (or sampling frequency) is critical and is determined by the amount of signal information that is needed for a given application. The sampling rate must be at least twice the highest frequency of the continuous signal in order to provide enough accurate samples to reconstruct the original signal. The sampling period is the time between samples ( $t_1$ ) and is defined by the minimum  $t$  (the inverse of twice the highest frequency) divided by the precision of the discretization. For instance, since we work with normalized image resolution values  $-f_{max}$  is 1 and  $f_{min}$  is 0.05 and correspondingly sampling rates could be 0.05, 0.5 and 1sec. Figure 3.18 in Section 3.5 illustrates how the number of samples per time unit taken from the continuous signal are generated.

### 3.4.2 Classification Logic

Hand joints classification is based on cross-correlation, a signal-processing technique for matching the similarity between signals. The observed current frame waveform for a potential hand joint is matched by cross-correlation to hand joint profiles in the DB, presented in format1 of Fig.(3.8d). Measuring cross-correlation is organized by two classifiers in a hierarchical way. The first one compares the data sequence  $x(n)$  sampled from the current features to each profile  $y(n)$  in the DB using the Eq.(3.5). Cross-correlation of the two input signals produces a third signal  $CC(n)$  obtained by averaging the sum of products of the corresponding pairs of  $N$  sampling points taken.

$$CC(n) = \frac{1}{N} \sum_{n=0}^{N-1} x(n) \times y(n) \quad (3.5)$$

We analyze the number of negative samples in  $CC(n)$  and continue with the second classifier only if the negative samples are less than five. If the number is more than

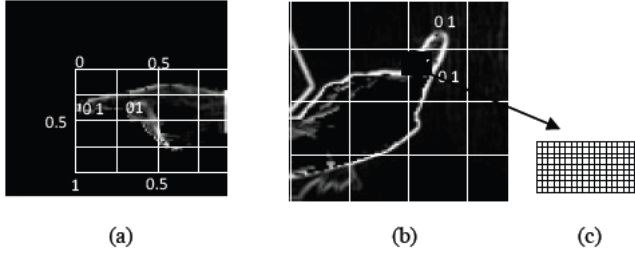


Figure 3.9: Adjacent to hand grid: (a)  $0.15 \times 0.15$  cell, (b)  $0.25 \times 0.25$  cell and (c)  $19 \times 9$  neighborhood mask.

five, the cross-correlation coefficient ( $CCoeff$ ) of the two signals is very small and it is not worth any calculations. We calculate  $CCoeff$ , which lies between  $-1$  and  $+1$ , from Eq.(3.6) in order to obtain a grade of similarity. The value of  $+1$  means 100% similarity, while small values indicate very low correlation.

$$CCoeff = \frac{\sum_{n=0}^{N-1} (x(n) - \bar{x}) \times (y(n) - \bar{y})}{\sqrt{\sum_{n=0}^{N-1} (x(n) - \bar{x})^2 \times \sum_{n=0}^{N-1} (y(n) - \bar{y})^2}} \quad (3.6)$$

where  $\bar{x}$  and  $\bar{y}$  are the means of  $x(n)$  and  $y(n)$ , respectively.

### 3.4.3 Positioning and Timing Information

Once the hand joints are identified and classified, the HGR framework positions them using binary encoding corresponding to their locations in a hand according to their positions in a grid adjacent to the segmented hand. It has  $4 \times 4$  cells and takes the size of the segmented hand. We use  $COG\_D(x, y)$  coordinates for tuning the size of the grid to end the wrist in order to increase the precision for localizing fingertips since some of the wrist and finger hand joints show equal wave profiles. Moreover, the cells where  $COG\_D$  and the fingertip are positioned help us to define the hand direction. Most researchers assume that the hand is always pointing upward but this is not true. For instance, in Fig.(3.9a), we compare the grid cells where  $COG\_D$  and a hand joint of type FingerTipPointing by simple logic to detect a left oriented hand. We define a pattern of bits to describe the HJ location that is relative to the adjacent grid. The corresponding decimal number is used at the gesture recognition phase. At the beginning, the HJ Location (HJL) consists of only zeros - "0" and when we classify a HJ (e.g. the presence of a finger) we assign a one - "1" according to  $(x, y)$  coordinates of neighbor pixels. For instance, if the adjacent to hand grid has  $100 \times 100$  pixels the HJL1 in Fig.(3.9a) has 01 at position  $x$  in the range  $[0, 0.25]$  and  $y$  in the range  $[0.25, 0.5]$  because there are overlapping grayscale patterns. The following figures show the tracked HJs in the different cells in hand grids and the pattern of bits for the HJ location.

HJL1=20480 (corresponding decimal)														
0	1	0	1	0	0	0	0	0	0	0	0	0	0	0
HJL2 = 4 (corresponding decimal)														
0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
Mask (above) = 255														
0	0	0	0	0	0	0	0	1	1	1	1	1	1	1
Mask (rightOf) =3840														
0	0	0	0	1	1	1	1	0	0	0	0	0	0	0

Figure 3.10: Feature locations and masks for relations.

```

Gestures.push({name:"OK", min_fingers:1, HJs:" thumb, fist", beginning_relation:"above",
beginning_HJs:"thumb, fist", ending_relation:"above", ending_HJs:"thumb, fist", runtime:
1000});

```

Figure 3.11: Pseudo code for gesture description in VG.

### 3.4.4 Recognition of a Hand Gesture

We incorporate the positions of segmented fingers and a palm with semantic keywords to define the meaning of the gesture. A gesture might consist of one pose (static gesture) or more poses (dynamic gesture). A pose consists of HJs and their spatial relations for some period of time. At the recognition phase, we use a Visual Grammar (VG) formalism proposed in [16] to describe the decomposition of a gesture into its poses, poses into hand joints and their spatial relations to each other over some period of time. Each sentence is composed of a set of elementary objects, which are connected by binary relations, e.g. the relationships of hand joints to each other. We define an enumeration JointRelationship to describe the possible relationships of joints that are supported by the VG, such as “above”, “leftOf”, “aboveAndRight”, and “belowAndLeft”. The pose description is incorporate in the gesture description with beginning and ending objects, see the description of gesture “OK” in Fig.(3.11). The gesture is static because the instances for the objects *beginning\_HJs* and *beginning\_relation* are the same as *ending\_HJs* and *ending\_relation*.

The reasoning process for gesture recognition is based on comparing the beginning and ending HJs and evaluating of the beginning and ending relations according to the HJs locations during the gesture runtime. Locations are binary numbers according to the HJ position in the adjacent grid. The “1” in the 13th and 15th bit in HJL1 in Fig.(3.10) indicate that there is “aboveAndLeft” oriented feature. To evaluate location relation, we use bit-wise operations (AND, OR, masking and bit shifts) that operate on the binary representation of an integer that characterize the HJ positions in the grid. Location matching is based on logical AND on each pair of bits from the HJL1 and HJL2. The mask above in Fig.(3.10) (- 255) helps in recognizing the “up” oriented HJ. By applying the mask above to HJL2 we establish whether the second hand joint is below the first one. Figure 3.12 shows a pseudo code how the relation above between the two hand joints HJ1 and HJ2 with corresponding bit patterns about their locations

```

function relation_above(HJ_type HJ1, HJ_type HJ2, Location HJL1, Location HJL2 ):Boolean{
if (HJL1 >=16384) //the first HJ is UP positioned
mask_HJL2=255;//0000000011111111
one of the bits [6,4,2,0] MUST be 1;
HJL2_masked =HJL2 & mask_HJL2;
//check the second bit in HJL2 ;
if((HJL2_masked >> 2) &1) = =1 return TRUE; }

```

Figure 3.12: Pseudo code how relations in VG sentences are evaluated.

HJL1 and HJL2 is evaluated to be true or false.

## 3.5 Implementation and Experimental Results

In this Section, we present in brief how the proposed HGR framework is implemented by interfacing Adobe AIR 3.0 with Kinect sensor. We provide the algorithm for clustering the depth stream, as well as parts of as3 source codes for RGB bitmap data preprocessing, feature identification and profiling, and cross-correlation of the observed waves to profiles in the DB. For verification and comparison of the proposed HGR framework, we use the hand gesture dataset collected by a Kinect sensor in [30] and provided online in [4]. Experimental results and discussion follow.

Since the input data for the proposed HGR framework is low level depth and RGB Kinect streams we use Kinect Native Extension with Adobe AS3 software (AIRKinect) developed by [35]. It has a lot of built-in features from light level functions that provide an abstraction layer with a generic interface to those two sensors to APIs that use the rich experience of the Microsoft Kinect. The drivers, installation directives and application libraries for interfacing Kinect with Flash&AS3 can be found in [35]. How to get started with installation of Kinect drivers and application libraries for the MS SDK version of the Kinect sensor for interfacing Kinect with AS3, as well as a simple AIRKinect application rendering the depth image, can be found on the site developed by us [2].

### 3.5.1 Implementation of HGR Framework

The AIRKinect-based application returns depth and color data using the following frame events `CameraImageEvent.DEPTH_IMAGE_UPDATE` and `CameraImageEvent.RGB_IMAGE_UPDATE`, which fire each time when new frame is available from the sensor. For each frame, we check whether the number of clusters in the current frame is different to the number in previous frame, and if this is true we continue with processing the depth stream and RGB bitmap, see Fig.(3.4).

#### 3.5.1.1 Coordinate systems

The Kinect sensor uses a laser grid to calculate depth map Fig.(3.5b) from IR image Fig.(3.5a). Microsoft Kinect SDK [7] uses two different coordinate systems: a skeleton

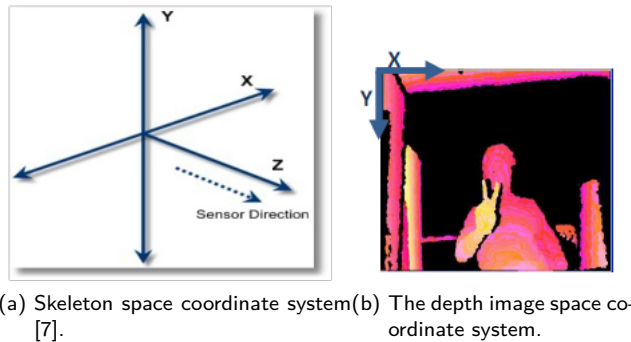


Figure 3.13: Coordinate systems in Microsoft Kinect for Windows SDK.

coordinate system and a depth image space coordinate system. The skeleton coordinate system as shown in Fig.(3.13a) places a Kinect at the origin with the positive  $z$ -axis extending in the direction in which the Kinect is pointed. The positive  $y$ -axis extends upward and the positive  $x$ -axis extends to the left. The three coordinates are expressed in meters. The depth and RGB image space coordinate system, refer to Fig.(3.13b) has its origin in the left upper corner of the image with the  $x$ -axis pointing right and the  $y$ -axis pointing down. For each frame, the depth sensor captures everything visible in the field of view, provided as a grayscale image or as a stream, consisting of only  $z$  coordinates expressed depth in millimeters. The image resolution specifies the length of depth stream.

To simplify the bitmap analysis of the grayscale image to get the depth values, we parse the depth stream and transform it to 2D array of pixels. In order to repeat and compare the experiments provided by different approaches that use dataset provided in [4], we show in Fig.(3.14) how to get the  $(x, y)$  coordinates for the depth values from the text files with depth streams as in [4]. The process of the depth stream in XYZ array in AIRKinect can be found in our site [2].

### 3.5.1.2 Preprocessing of depth raw data

The input to LCFC algorithm for clustering of depth data is the  $z$  coordinate, i.e., the depth value for each pixel normalized according to  $\text{minDepth}$  and  $\text{maxDepth}$ . The full sources can be found in [2] in the topic: Download, while the explanations on how to vary the LCFC thresholds for coarse and fine clustering can be seen at the topic: Clustering.

### 3.5.1.3 Preprocessing of color raw data

RGB raw data needs to be preprocessed before passing to LCFC algorithm for categorizing them. The bitmap data handled during the event `CameraImageEvent.RGB_IMAGE_UPDATE` initializes an array named `input_RGB`, as shown in Fig.(3.15).

In scenarios where the hands are not the most front objects, we first perform skin region segmentation to find the `COG_rgb` for the segmented hand using formulae in

```

function loaderCompleteHandler(event:Event) : void
{
    //loading the depth streams as text files
    loader.removeEventListener(Event.COMPLETE, loaderCompleteHandler);
    parse(loader.data)
}
var lines:Array = data.split('\n'); //split data file by lines (height)

for(i=0;i<height;i++)
{
    tabs[i] = lines[i].split(","); //split data file by comas (width)
    depth_data[i] = lines[i].split(",");
}

//then we need to rotate the bitmap by 90°
for(i=0;i<height;i++)
{
    for(var j:int=0;j<width;j++)
    {
        depth_data[j][i]=tabs[i][j];
        //trace(depth_data[j][i]);
    }
}
}

```

Figure 3.14: Part of as3 code for parsing of the depth text files in [4].

```

protected function onRGBImageUpdateHandler(event:CameraImageEvent):void
{
    _rgbBitmap.bitmapData = event.imageData;
    input_RGB=new Array();
    var i:int = 640 * 480;
    while ( i-- )
    {
        //this is the position of each pixel in x & y
        x1 = i % 640;
        y1 = int( i / 640 );
        color = _rgbBitmap.bitmapData.getPixel( x1, y1 );
        input_RGB[x1][y1]=color; //to trace color: trace(input_RGB[x1][y1].toString(16));
    }
}
}

```

Figure 3.15: Part of as3 code for RGB bitmap data handling.



-1	0	+1	+1	+2	+1
-2	0	+2	0	0	0
-1	0	+1	-1	-2	-1
$G_x$			$G_y$		

$$|G| = |G_x| + |G_y|$$

Figure 3.16: Sobel convolution kernels,  $G$  - approximate gradient magnitude.

Fig.(3.7). Then we detect edges by Sobel gradient measurement. The Sobel operator [14] consists of a pair of  $3 \times 3$  convolution kernels as shown in Fig.(3.16). The second kernel is simply the first rotated by  $90^\circ$ . As3 code showing how to apply the Sobel operator to the bitmap data for edge detection is expressed in Fig.(3.17).

We convert  $BMD\_edges$  from RGB to HSV format, see Fig.(3.6); and the V values together with  $(x, y)$  pixel coordinates of the segmented hand are made the inputs to LCFC algorithm. The clustering thresholds for processing color data in our implementation are:  $MDthr = 0.4$  and  $Mthr = 0.07$  resulting in about 40-55 number of clusters and average 5-8 overlapped clusters. The size of the neighborhood mask is  $19 \times 9$  pixels and the clusters are ordered by their  $x$  coordinates.

#### 3.5.1.4 Implementation of hand joint profiling and signals cross-correlation

Figure 3.18 illustrates how the number of samples are taken from the continuous signal. With a sampling period of  $t_1 = 0.05$  the accuracy of the corresponding digital signals is better; however this will increase the size of DB and the time for responding. The  $t_1 = 0.5$  gives enough precision in only 42 samples per profile. The pseudo code, mainly given to illustrate the input format of waves for cross-correlation, shown in Fig.(3.19), explain how to add the individual sine waves with amplitudes  $A_i$  and frequencies  $f_i$  for calculating  $S(t)$ .

Measuring the similarity between signals by cross-correlation is organized by two classifiers in a hierarchical way. First we measure cross-correlation between the observed and trained, in the DB, waves that produces a third wave  $CC(n)$ . Then we analyze the number of negative samples in  $CC(n)$  and if it is less than 5 and the minimal amplitude of  $CC(n)$  is in the range  $[-0.05, 0.2]$  we calculate cross-correlation coefficient ( $CCcoef$ ) of the two signals by Eq.(3.6) in order to obtain the grade of similarity. Implementation is shown in Fig.(3.20).

The DB consists of 6940 profiles, while the VG consists of 18 sentences. According to the recognized poses and their timestamps, the rotation angles for the motors of the robot hand(s) are updated, however this is a scope of another study.

### 3.5.2 Experiments

During the testing phase, we match a potential hand joint wave to the preprocessed hand gesture of the trained data in the DB. They are collected during the training

```

function SobelEdgeCalculation(w:int, h:int,BMD_rgb:Array) {
  for (row = 1; row < w; row++){
    for ( column = 1; column < h; column++){
      m11 = GrayTransf(BMD_rgb [row-1][column-1]);
      m12 = GrayTransf(BMD_rgb [row][column-1]);
      m13 = GrayTransf(BMD_rgb [row+1][column-1]);
      m21 = GrayTransf(BMD_rgb [row-1][column]);
      m22 = GrayTransf(BMD_rgb [row][column]);
      m23 = GrayTransf(BMD_rgb [row+1][column]);
      m31 = GrayTransf(BMD_rgb [row-1][column+1]);
      m32 = GrayTransf(BMD_rgb [row][column+1]);
      m33 = GrayTransf(BMD_rgb [row+1][column+1]);

      Gx = -m11+m13-2*m21+2*m23-m31+m33;
      Gy = m11+2*m12+m13-m31-2*m32-m33;

      G = Math.abs(Gx)+Math.abs(Gy); // G *= 0.5;
      newPixel= (G<< 16) + (G << 8) + G;
      BMD_edges[row][column]=newPixel;
    }
  }
}

function GrayTransf(px:uint):uint {
  var red:uint = (px >> 16 & 0xFF);
  var green:uint = (px >> 8 & 0xFF);
  var blue:uint = (px & 0xFF);
  // Any color is obtained by mixing the three primary colors in suitable proportions
  return (red* 0.30 + green* 0.59 + blue* 0.11);
}

```

Figure 3.17: Part of as3 source code for edge detection by the Sobel algorithm.

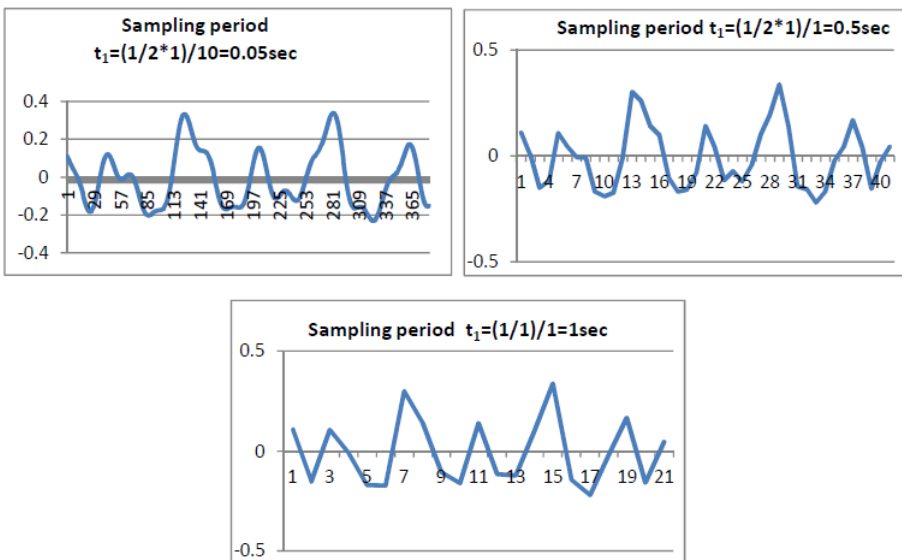


Figure 3.18: Variation in the number of samples taken from a continuous wave to describe it as a discrete wave.

```

Inputs: arr [] - array of struct with parameters for overlapping_clusters
          sampling period  $t_1 = 0.5\text{sec}$ ,  $t_i = t_{i-1} + t_1$ 
//clusters parameters-> Nexamples:number of examples; arr[1].color: color
if(arr.length==6) {
  for(i=0;i<42;i++) {
    FM[i]=arr[0].Nexamples*Math.sin(2*Math.PI*arr[0].color*t[i])+
    arr[1].Nexamples*Math.sin(2*Math.PI*arr[1].color*t[i]+Math.PI/4)+
    arr[2].Nexamples*Math.sin(2*Math.PI*arr[2].color*t[i]+Math.PI/2)+
    arr[3].Nexamples*Math.sin(2*Math.PI*arr[3].color*t[i]+3*Math.PI/4)+
    arr[4].Nexamples*Math.sin(2*Math.PI*arr[4].color*t[i]+Math.PI)+
    arr[5].Nexamples*Math.sin(2*Math.PI*arr[5].color*t[i]+3*Math.PI/2);
  }
}

```

Figure 3.19: Pseudo code for calculating  $S(t)$ .

```

Input: FM and the number of the simple sinusoids in the wave
function cross_correlation(number:int,FM:Array):Number {
  // Implementation of Eq(3) for all c records in DB
  for( c=0;c<DB.length;c++){
    cnt_neg=0;//counter for negative values in CC(n)
    Di=FRB[c].concat();
    for(d=0;d<Di.length-1;d++) {
      CC[d]=Di[d]*FM[d];
      if (product[d] < 0.0)
        cnt_neg++;
    }
    for(d=0;d<Di.length-2;d++) {
      if (minAmplitudeCC>CC[d])
        minAmplitudeCC =CC[d];
    }
    if( cnt_neg<10 && minAmplitudeCC <=-0.0 && minAmplitudeCC >=-0.2 )
      CCcoef [c]=0.75;
    if( cnt_neg<10 && minAmplitudeCC <=-0.2 && minAmplitudeCC >=-0.4 )
      CCcoef [c]=0.5;
    if( cnt_neg<5 && minAmplitudeCC <=0.0 && minAmplitudeCC >=-0.05 ) {
      //Implementation of Eq. (4)
      for(d=0;d<Di.length-1;d++) {
        mean1=mean1+Di[d];
        mean2=mean1+FM[d];
      }
      mean1=mean1/Di.length;
      mean2=mean2/Di.length;
      for(d=0;d<Di.length-1;d++) {
        nomin=nomin+(Di[d]-mean1)*(FM[d]-mean2);
        denom1=denom1+(Di[d]-mean1)*(Di[d]-mean1);
        denom2=denom2+(FM[d]-mean2)*(FM[d]-mean2);
      }
      CCcoef [c]=nomin/(Math.sqrt(denom1*denom2));
    }
    Di.splice(0);
  } //ending with all profiles in DB for current size
  return (the_max_to_all_DBprofiles_CCcoef);
}

```

Figure 3.20: Pseudo code for wave's cross-correlation.

Table 3.1: Overall Accuracy for gestures: “Pointing” (G2), “Number\_two” (G3), “Hi” (G6), “Ok” (G9).

Gesture	cases	tp	Acc
G2 all 10 Subjects	40	38	0.95
G3 all 10 Subjects	40	36	0.90
G6 all 10 Subjects	40	33	0.82
G9 all 10 Subjects)	40	38	0.95

phase from hand gesture dataset taken by a Kinect sensor [30] and given online[4]. Dataset is collected from 10 subjects, each containing 10 gestures and 10 different poses for the same gesture, so in total the dataset consists of 1000 cases, each of which consists of a color image and a depth map. The gestures are static and taken in different views, backgrounds, and variations in a gesture pose, illumination, skin color, sizes and shapes. We trained and tested the performance of our HGR framework only for four gestures from the dataset, collected from all 10 subjects in 10 different poses for the same gesture, so in total we exploit 400 cases. We use the first six poses from all subjects to train the DB, and the last four poses to test the accuracy of our HGR framework. The types of gestures we identified are: “Pointing” – gesture G2; “Number\_two” – gesture G3; “Hi” – gesture G6 and “Ok” – gesture G9.

Our training phase has taken 240 cases from all 10 subjects, with the first 6 poses taken for all 4 gestures. After hand segmentation according to the depth stream and preprocessing of color information given for each pose, we identify about 25-30 grayscale patterns in short distance featuring HJs. A hand joint may be identified by more than one grayscale pattern, for instance, about 6 profiles specify a spread finger and more than 10 categorize folded fingers that present in all four gestures. After profiling and labeling these features with the relevant type of HJ, we recorded them in the DB. However, self-signal cross-correlation needs to be performed first to remove duplicated wave profiles. The current DB consists of 1810 wave profiles for the gesture G3 and 6940 for the all four gestures. The VG consists of 18 sentences. The sentences combined a type of finger(s), one or two relations with palm, folded fingers or wrist. For instance, the sentences for “Ok” gesture are 3. A thumb and the relation “above” combined with three HJs: palm, wrist or folded fingers (fist).

### 3.5.3 Results and Discussion

In the context of classification tasks, accuracy represents the percentage of recognitions that are correct. The terms true positives ( $tp$ ) and false positives ( $fp$ ) are used to compare the given classification of the HGR framework with the desired correct classification. Correct gesture recognition is taken as “ $tp$ ”. Overall accuracy is calculated by Eq.(3.7).

$$Acc = \frac{tp}{tp + fp} = \frac{tp}{total\ number\ of\ cases} \quad (3.7)$$

Table 3.1 illustrates the accuracy in recognizing the four gestures. The testing cases

are the last four poses for each gesture taken from all subjects – 40 cases per gesture. The overall accuracy is 90%. It shows that the proposed HGR framework needs a small number of cases during the training to start recognizing a new gesture with a feasible accuracy – only 240 cases and about 1810 wave profiles in the DB. Moreover, still during the training and feeding to our DB with HJ profiles for the gesture G3, we observed that only by 60 poses we obtain 80% accuracy in recognition. We use 160 cases at the testing phase - from all 10 subjects, the last 4 poses taken for all 4 gestures. We establish that the accuracy in recognition of spread fingers (index, middle or ring) and in thumb is about 95%. The subject is irrelevant however the orientation of the hand is important. For instance, the cases with no upward-oriented hand in G3 are less than upward-oriented ones and consequently they are less recognizable. The worst recognition accuracy shows gesture G6. We explain this with the fact that the training poses for this gesture are not enough to distinguish between index, middle and ring fingers, which participate in the VG sentences for “Hi” gesture description. We matched at least 5 HJs profiles for fingers in the VG sentence however, we are not sure what type of fingers participate (index, middle or ring) since they have similar profiles. We will solve this problem in the future with more detailed study of HJs positions in accordance to the adjacent to the hand grid. The reason for less recognition accuracy for gesture G3 could be attributed to the quantization errors in depth camera and low Kinect resolution that limit our classification when a finger is dropped. A human eye cannot see a dropped finger however, in case a finger is not dropped at all, a grayscale pattern exists and the DB has been trained with such profiles. We can then later recognize the low resolution cases. Another reason for dropping could be related to when the subject is in “Kinect near mode” and the finger is closer to Kinect than the minimum depth threshold. The good thing is that we always distinguish fingers than the other hand joints and unpredictably we recognized the folded fingers present in all 4 gestures with an accuracy of 97%, which will be very useful in the future for recognizing complex dynamic gestures.

We plan to improve the overall accuracy of the proposed HGR framework in the future by training it with much more profiles derived from gestures varying in hand sizes, shapes and poses together with the enhanced in resolution of new Kinect sensors. We followed the lessons from Microsoft Kinect and Leap to design accurate data-driven software algorithms for gesture recognition [12]. The extremely low cost of CPU and GPU cycles permits now to throw large amounts of Kinect data at the computer and let the algorithms figure out from a large set of tagged data and decide which attributes (features) are important for making the recognition decisions. We also discovered how to determine which feature provides the most valuable information and how to reduce the data for identification by clustering light intensity on hand edges. However, a DB optimization is required when the HGR framework is applied in a local mode on a robot side. The framework can easily be extended for more gestures. The system response time depends on the clustering time and the numbers of waves in the DB, but not on the HJ position and orientation because that does not affect its size. DB does not contain the positions of features for hand joints.

## 3.6 Conclusions

The recent study proposes a new way of understanding and interpreting gestures by robots, and therefore opening up a number of research opportunities in the field of designing smart sensors derived from the radar technology using a signal in the optical range of the electromagnetic spectrum to perform signal processing. The proposed hand gesture recognition framework can be applied to different measurable signals that are proportional to infrared or visible light radiation and is robust to lightening conditions, cluttered backgrounds and hand sizes, shapes and poses by exploiting grayscale patterns for the regions with the high change in light intensity obtained by online low-complexity constrained fuzzy clustering and reasoning. The framework has been applied to row data obtained by Microsoft Kinect IR and RGB sensors and the result clustering, features identification and a novel profiling resolved some of the problems that researchers met when using Kinect sensor for hand gesture recognition. The framework might be implemented in two scenarios as a local hardware solution practicable when the sensor is placed on a robot side or as wireless software application practicable for remote gesture recognition. In the future we plan to design the proposed grid of nano-antennas in a network simulator, as well as in a network emulator, and test the overall distributed process for preprocessing and clustering of the harvest infrared and visible light converted to electric current signals.

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